## Subject Code: R10107/R10

I B.Tech I Semester Supplementary Examinations Nov./Dec. - 2015
MATHEMATICAL METHODS
(Common to CSE, EEE, CE, EIE, AE, BT \& MM)
Time: 3 hours
Max. Marks: 75

## Answer any FIVE Questions All Questions carry equal marks <br> $* * * * *$

1. (a) Solve the system of equations $x+3 y+2 z=0,2 x-y+z=0,3 x-5 y+4 z=0, x+17 y+4 z=0$
(b) Find the Rank of the matrix $\left[\begin{array}{llll}0 & 1 & 2 & 2 \\ 1 & 1 & 2 & 3 \\ 2 & 2 & 2 & 3 \\ 2 & 3 & 3 & 3\end{array}\right]$ using Normal form.
[8+7]
2. (a) Find the Eigen values and Eigen vectors of the Matrix $\left[\begin{array}{ccc}1 & 2 & -2 \\ 1 & 1 & 1 \\ 1 & 3 & -1\end{array}\right]$
(b) Verify Cayley- Hamilton Theorem for the matrix $\left[\begin{array}{lll}1 & -2 & 2 \\ 1 & -2 & 3 \\ 0 & -1 & 2\end{array}\right]$ Hence find $A^{4}$ and $A^{-1}$
3. Find the Rank, signature and index of the quadratic form $2 x^{2}+y^{2}-3 z^{2}+12 x y-4 x z-8 y z$ by reducing into canonical form
4. (a) Solve the equation $x-\cos x=0$ using Bisection Method
(b) Solve the equation $x^{3}-8 x-4=0$ using Iteration Method
5. (a) Find $y$ (1.6) from the following table

| x | 1 | 1.4 | 1.8 | 2.2 |
| :--- | :--- | :--- | :--- | :--- |
| y | 3.49 | 4.82 | 5.96 | 6.5 |

(b) Find $y(10)$ if $y(5)=12, y(6)=13, y(9)=14, y(11)=16$
6. (a) Compute the first derivative for the following data at $\mathrm{x}=-3$ and $\mathrm{x}=0$

| X | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | -33 | -12 | -3 | 0 | 3 | 12 | 33 |

(b) Evaluate $\int_{4}^{5.2} \log x d x$ using (i) Trapezoidal rule (ii) Simpson $1 / 3$ rule

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Set No-1
7. (a) Evaluate $y(0.1), y(0.2)$ by Taylor's Series method given that $y^{1}=x+y^{2}, y(0)=1$ (b) Evaluate $y(0.25), y(0.5)$ by RK method given that $y^{1}=x^{2}+y^{2}, y(0)=1$
8. (a) Derive Normal Equations to fit the straight line $y=a x+b$
(b) Fit the curve $y=a+b x+c x^{2}$ for the following data

| X | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 2.98 | 4.26 | 5.21 | 6.10 | 6.80 | 7.50 |

